

Please write clearly in	n block capitals.	
Centre number	Candidate number	
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# GCSE MATHEMATICS

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Higher Tier Paper 2 Calculator

Wednesday 7 June 2023 Morning Time allowed: 1 hour 30 minutes

#### **Materials**

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).

#### Instructions

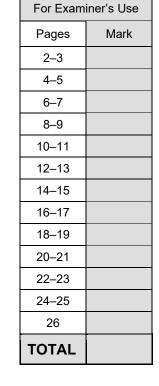
- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

#### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

#### **Advice**

In all calculations, show clearly how you work out your answer.





	Answer <b>all</b> questions in the spaces provided.	
Write	30:12 in the form n:1	[1 mark]
	Answer: 1	
	consecutive triangular numbers are 6 10 15 21 down the next triangular number.	[1 mark
	Answer	



Write down the reciprocal of $\frac{4}{7}$	
	[1 mark]
Answer	
The price of a toy increases by 12.5% to £19.53	
Work out the <b>original</b> price of the toy.	[2 marks]
Answer £	

Turn over for the next question





Jess saves 2p, 5p and 10p coins.	
She has	
• 45 10p coins	
8 times as many 2p coins as 10p coins	
• £17.70 in total.	
Work out total <b>value</b> of 2p coins : total <b>value</b> of 5p coins	
Give your answer in its simplest form.	
	[4 marks]
Answer :	

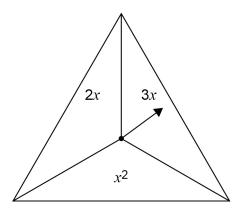


Assume that the polygon is an octagon.  Work out the size of an exterior angle.  [2 marks]  Answer	6 (a)	Part of a regular polygon is shown.	Not drawn accurately	Do not wr outside th box
6 (b) In fact, the polygon has more sides than an octagon.  What does this mean about the size of an exterior angle?  Tick one box.  [1 mark]  It is more than the answer to part (a)			[2 marks]	
Tick <b>one</b> box.  [1 mark]  It is more than the answer to part (a)  It is the same as the answer to part (a)	6 (b)		o	
It is the same as the answer to part (a)			[1 mark]	
		It is more than the answer to part (a)		
It is less than the answer to part (a)		It is the same as the answer to part (a)		
		It is less than the answer to part (a)		



box

- 7 In a game,
  - an ordinary fair six-sided dice is rolled
  - the fair spinner shown is spun.



The score is the dice number **substituted** into the spinner expression.

7 (a) Complete the table to show all of the possible scores.

[2 marks]

	1	2	3	4	5	6
<b>2</b> x				8		
<b>3</b> <i>x</i>		6				
$x^2$					25	

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7 (b) A player wins the game if their score is 10 or more.

Work out the probability that they win the game.

[1 mark]

Answer

7 (c) The game is played 711 times.

Estimate the number of games that are won.

Answer

[2 marks]

8  $(a-3)x^2 + 2b \equiv 5x^2 + 12$ 

Work out the values of a and b.

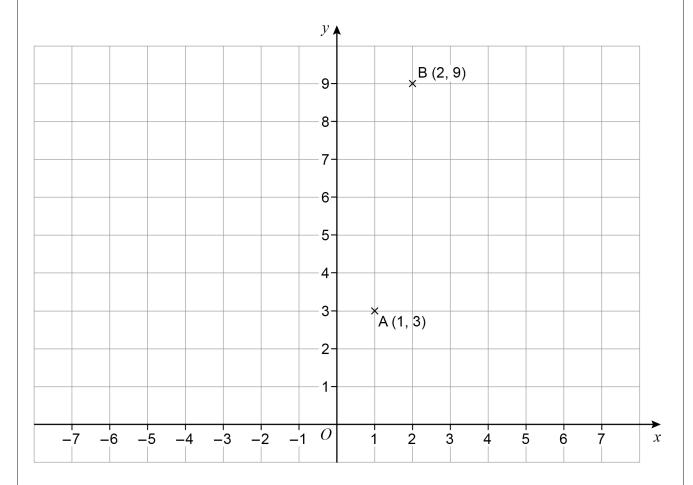
[2 marks]

$$a = b =$$

7



**9** A (1, 3) and B (2, 9) are points on a centimetre grid.



ABCD is a parallelogram.

AD and BC are **horizontal** and each has length 5 cm

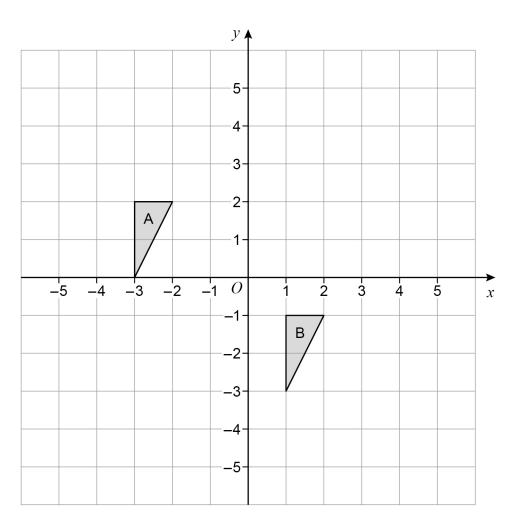
The diagonals of ABCD cross at E.

Work out the <b>two</b> possib		[4 marks]		
Answer (	,	) and (	,	)



Write down the translation vector that maps shape A onto shape B.

[2 marks]



∆nswer			
411 <b>5</b> WH			

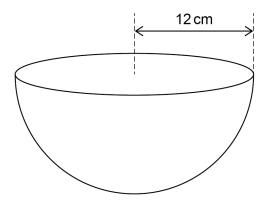
6



11

Volume of a sphere = 
$$\frac{4}{3}\pi r^3$$

A bowl is a hemisphere with radius 12 cm



Water is poured into the bowl at a rate of 325 cm<sup>3</sup> per second for 8 seconds.

Does the water fill more than 70% of the bowl?

You must show your working.

•	J		[4 marks]



Show that these two rectangles are similar.  [2 marks]  Not drawn accurately		
5 cm 8 cm 12 cm 19.2	2 cm	
A factory packs $x$ boxes of teabags per hour. Each box contains 80 teabags. Show that the factory packs $\frac{4x}{3}$ teabags per minute.	[2 marks]	



box

**14** A company has 123 employees.

Information about their hourly rates of pay is shown in the table.

Hourly rate, £p	Number of employees
10 ≤ <i>p</i> < 14	66
14 <i>≤ p</i> < 20	32
20 ≤ <i>p</i> < 40	15
40 ≤ <i>p</i> < 100	10
	Total = 123

The owner of the company uses the data to make two statements.

### Statement A

"Over 30% of employees have an hourly rate that is more than £17"

## Statement B

"The average hourly rate of pay is more than £20"

14 (a)	Show working	that supports	Statement A.
--------	--------------	---------------	--------------

[3 marks]



14 (b)	Why might <b>Statement A not</b> be true?	[1 mark]	Do not write outside the box
14 (c)	Work out an estimate of the mean to support <b>Statement B</b> .	[3 marks]	_
14 (d)	Why is the mean <b>not</b> the best average to represent the data?	[1 mark]	



15	Expand $(x^2 - 9xy)(2x + 5y)$	[2 marks]
	Answer	
16	Line A has equation $y = ax - 1$ passes through the point (7, 13)	
	Line B has equation $5y - 3x = 4$ Show that line A has a greater gradient than line B.	[3 marks]



**17** Not drawn 37° 9.3 cm 4 cm С

Do not write outside the box

accurately

Work out the size of angle x.

[4	ma	rks]
----	----	------



18	Rearrange	$y = \frac{x+8}{x}$	to make $x$ the subject.	[3 marks]
		Answer		
		7 11 10 11 01		

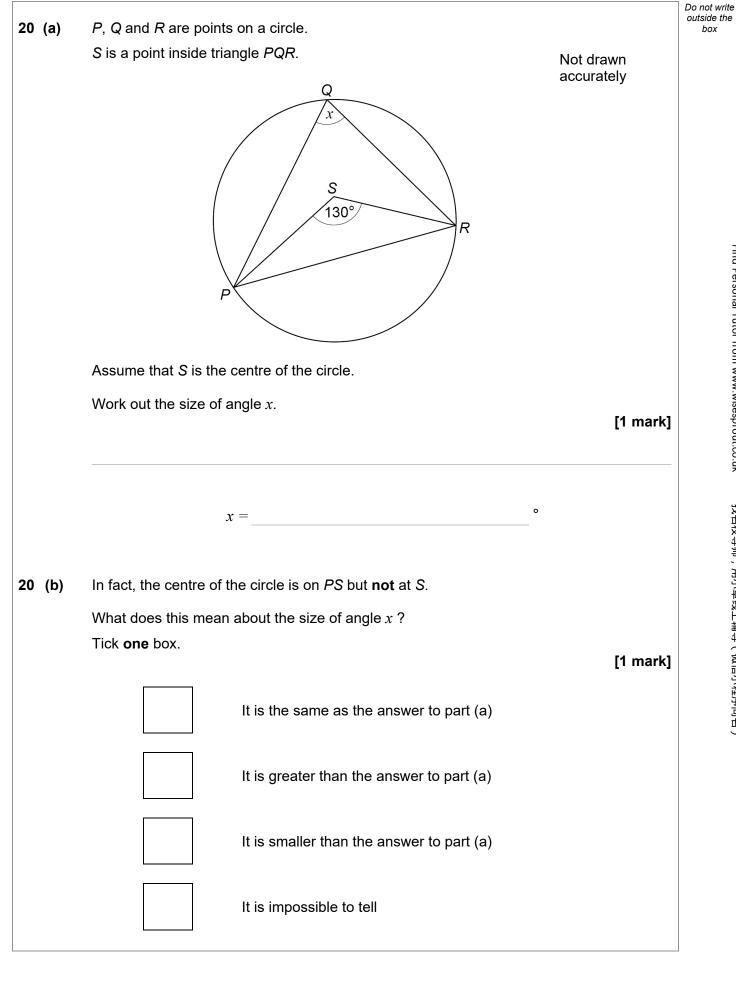


Here are	he firs	t four te	rms of a	quadratic s	equence.	
	3	20	47	84		
Work out	an exp	ression	for the n	th term of t	he sequence.	[4 marks]
		Δ				
		Answe	er			



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box



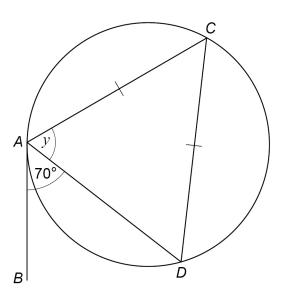


20 (c) For a different circle,

AB is a tangent at A

C and D are on the circumference of the circle

AC = CD



Not drawn accurately

Here is Simon's method to work out the size of angle y.

Angle 
$$ADC = 70^{\circ}$$
 (alternate segment theorem)

Therefore  $y = 70^{\circ}$  (angles in an isosceles triangle)

Is he correct?

Give a reason for your answer.

[1 mark]

L	



21	Magana decides to put £500 into an account that pays compound interest.	
- •		
	She wants to have at least £560 in the account after 3 years.	
	Work out to 1 decimal place the <b>minimum</b> annual interest rate she needs.	
	work out to 1 decimal place the <b>minimum</b> annual interest rate she needs.	[3 marks
		Į · · · · · · · · ·
	Answer %	



box

22 An approximate value of a root of an equation, x, can be found using the iterative formula

$$x_{n+1} = \sqrt[3]{5(x_n)^2 - 2x_n - 3}$$

The starting value is  $x_1 = 4$ 

**22** (a) Work out the values of  $x_2$  and  $x_3$ 

[2 marks]

 $x_2 =$ 

$$x_3 =$$

**22 (b)** By continuing the iteration, show that the value of x is more than 4.25

[1 mark]

\_\_\_\_\_



box

23 Here are three sets of cards.

Set A	1	1	3	5	5	5	6	8
-------	---	---	---	---	---	---	---	---

Set C	3	4		5	6
-------	---	---	--	---	---

In a game, a player has two options.

# Option 1

Pick two cards from Set A

# Option 2

Pick one card from Set B and pick one card from Set C

The cards are picked at random.

The player wins if the total of their two cards is exactly 10



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Which option gives a better chance of winning?	
Option 1 Option 2	
Show working to support your answer.	[4 marks
Turn over for the next question	





a=65 to the nearest integer $b=30$ to 1 significant figure	
Work out the <b>upper bound</b> for $2a^2 - b^2$	
You <b>must</b> show your working.	[2 mark
	[3 mark
Answer	



[3 marks]

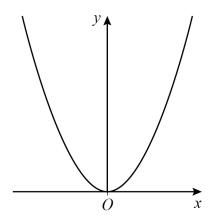
25	Show that	$\frac{x-5}{}$	x+5
	Officw triat	$\overline{x-2}$	
		2	

simplifies to  $\frac{ax^2-b}{x^2-4}$  where a and b are integers.

Turn over for the next question

6





**26 (a)** The minimum point of  $y = x^2$  is at (0, 0)

Write down the coordinates of the minimum point of  $y = x^2 + 2$ 

[1 mark]

Answer ( \_\_\_\_\_ , \_\_\_\_ )

**26 (b)** The graph  $y = x^2$  is reflected in the x axis.

Write down the equation of the graph after this transformation.

[1 mark]

Answer

**26 (c)**  $y = x^2$  is now transformed to give  $y = (x + 3)^2$ 

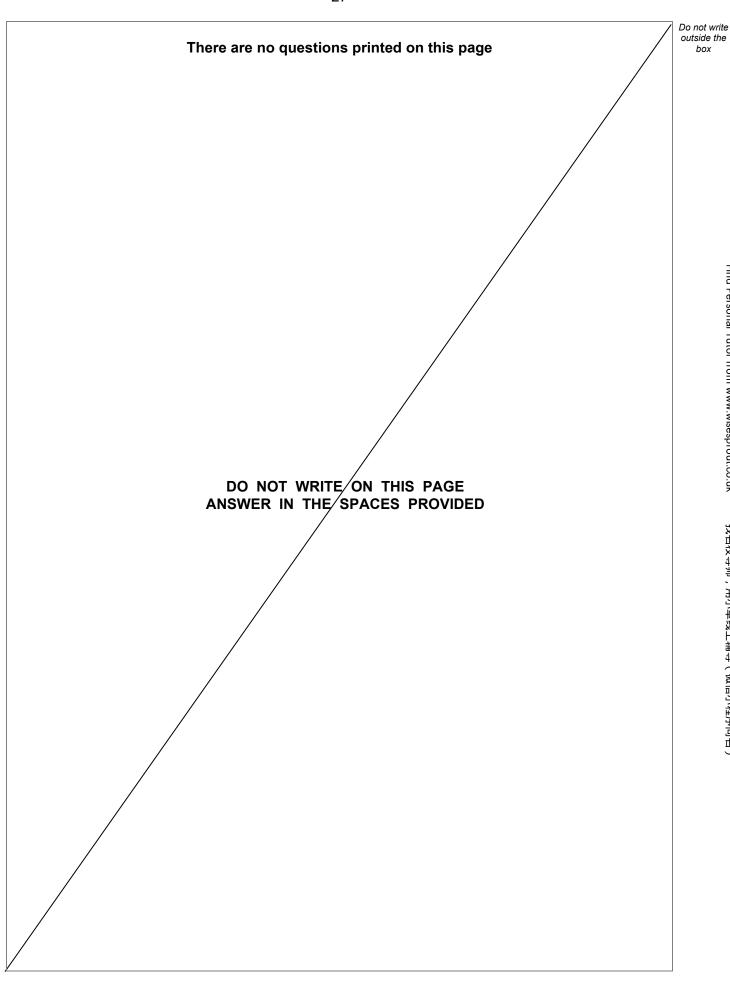
Describe fully this single transformation.

[2 marks]

# **END OF QUESTIONS**

4







Question number	Additional page, if required. Write the question numbers in the left-hand margin.



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